

Can a contract be signed on behalf of a trust still to be registered?

No. Such an agreement would be invalid.